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ABSTRACT: A realization of voltage-mode transfer functions with multiple feedback signal for third-order active-R filter using an operational amplifier has been presented. The single circuit gives three filter functions, low pass, high pass and band pass. This filter circuit can be used for different Q with high passband gain and ideal gain roll-off for higher Q values. The low pass and band pass performance of the circuit gives high passband gain and excellent GRPO for higher values of Q. For high pass filter, circuit shows gain stabilization at 0 dB for higher values of Q. Low pass, Band pass and High pass filter works excellent for higher values of Q.

Keywords: Filters; third-order; active-R; multiple feedback signal, passband.

I. INTRODUCTION

The operational amplifier (op. amp.) is now accepted as the basic active component for an inductor less filter. The circuit is realized using single pole (as “integrator”) behavior of an internally compensated operational amplifier.²,4,5,9 The filter without the capacitor is called an active-R filter [1]. This filter has received much attention due to its potential advantages in terms of miniaturization, ease of design and high frequency performance.³,6,8 This paper proposes realization and design method for third-order active-R filter with multiple feedback signals. This filter circuit gives three filter functions, low pass, high pass and band pass with ideal gain roll-off and high passband gain. The circuit is designed and studied for different values of circuit merit factor Q.

II. CIRCUIT CONFIGURATION

The proposed active-R third-order filter circuit diagram with multiple feedback is shown in figure-1. With the advent of the high frequency roll-off in the response of the op.amp, the circuit is constructed with multiple feedback.

There are three op.amplifiers (µ A741), with identical gain bandwidth product as an active element, and four resistances. This filter gives multiple outputs, which tend three filter functions, low pass, band pass and high pass. The negative feedback is introduced through resistances R1, R2, R3 from the output of the three op.amplifiers to inverting input of the first op.amp. The resistance R2 is tapped at different points for variation in feedback. The op.amps are coupled such that output of first op-amp is connected to non-inverting input of second op-amp and output of second op-amp is connected to non-inverting input of third op-amp. Non-inverting terminal of first op-amp, inverting terminal of third op-amp are grounded. The inverting terminal of second op-amp is connected to non-inverting terminal of first op-amp so that input V₄ appears at inverting terminal of second op-amp. The input is applied to inverting input of first op-amp through R₄.

III. CIRCUIT ANALYSIS AND DESIGN EQUATIONS

The single-pole model of an op.amp. leads to complex gain and the transfer function is given by [8].

\[ A(s) = \frac{A_o \omega_o}{(S + \omega_o)} \]

(1)

Where,

\[ A_o = \text{open loop d.c. gain}, \quad \omega_o = \text{open loop 3dB bandwidth}, \quad GB = A_o \omega_o = \text{gain bandwidth product of op.amp.} \]

\[ A(s) = \frac{A_o \omega_o}{S} = \frac{GB}{S} \]

(2)
Where, $S \gg \alpha_0$

This shows that the op. amp. is an “integrator”, Thus the active-R third-order filter transfer function at three different terminals are given below. The voltage transfer function for low pass filter.

$$T_{lp}(S) = \frac{-(1/R_1)GB_1GB_2GB_3}{X_1S^3 + X_2S^2 + X_3S + X_4}$$ \hspace{1cm} (3)

The voltage transfer function for band pass filter

$$T_{bp}(S) = \frac{-(1/R_1)GB_1GB_2S}{X_1S^3 + X_2S^2 + X_3S + X_4}$$ \hspace{1cm} (4)

The voltage transfer function for high pass filter

$$T_{hp}(S) = \frac{(1/R_1)S^3}{X_1S^3 + X_2S^2 + X_3S + X_4}$$ \hspace{1cm} (5)

Where,

$$X_1 = \left( \frac{1}{R_1} + \frac{1}{AR_2} + \frac{1}{R_3} - \frac{(1-A)MR}{A} \right)$$

$$X_2 = \left( \frac{1}{R_1} + (1-A)R_2M \right)$$

$$X_3 = (RM)$$

$$X_4 = \frac{GB_1GB_2GB_3}{R_3}$$

$$M = \frac{1}{A(1-A)R_2^2 + RR_2}$$

The circuit was designed using coefficient matching technique with general third-order filter transfer function $[4,5]$

$$T(S) = \frac{H_1S^3 + H_2S^2 + HS + H_0}{S^3 + S^2\alpha_0\left[(1/Q)+1\right] + S\alpha_0^2\left[(1/Q)+1\right] + \alpha_0^3} \hspace{1cm} (6)$$

By comparing (3), (4), and (5) with (6), we get the design equation as

1. $R_1 = \frac{P}{N - [(1-A)RM]}$

2. $R_2 = -X + \sqrt{X^2 + \frac{RN^2}{PA(1-A)}}$

Where $X = \frac{R}{2A(1-A)}$

3. $R_3 = N^3$

4. $R_4 = \frac{1}{1 - \frac{1}{R_1} - \frac{1}{AR_2} - \frac{1}{R_3} - \frac{(1-A)RM}{A}}$

Values of $R_1; R_2; R_3$, and $R_4$ can be calculated using these equations for different values $Q$ (table 1).

For practical realization all values of resistances are scaled by 100.
The circuit performance was studied with different values of $Q$ ($Q = 0.2, 0.5, 1.2, 2, 5, 10, 15, 20, 25$). The table 1 shows resistance values of resistance for different $Q$ value. The circuit was studied for different values of $Q$ for centre frequency $f_0 = 10$ KHz. The observed frequency response shows good agreement with theoretical results. Following observations are noticed from experimental study at three different terminals; low pass, band pass and high pass filter function for different $Q$.

### Table 1

<table>
<thead>
<tr>
<th>$Q$</th>
<th>$R_1$ $\Omega$</th>
<th>$R_2$ $\Omega$</th>
<th>$R_3$ $\Omega$</th>
<th>$R_4$ $\Omega$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>9.41</td>
<td>232.6</td>
<td>175.6 k</td>
<td>1.12</td>
</tr>
<tr>
<td>0.5</td>
<td>18.9</td>
<td>426.1</td>
<td>175.6 k</td>
<td>1.06</td>
</tr>
<tr>
<td>1.2</td>
<td>28.6</td>
<td>595.4</td>
<td>175.6 k</td>
<td>1.04</td>
</tr>
<tr>
<td>2</td>
<td>38.4</td>
<td>747.8</td>
<td>175.6 k</td>
<td>1.03</td>
</tr>
<tr>
<td>5</td>
<td>48.3</td>
<td>887.6</td>
<td>175.6 k</td>
<td>1.02</td>
</tr>
<tr>
<td>10</td>
<td>52.8</td>
<td>947.7</td>
<td>175.6 k</td>
<td>1.02</td>
</tr>
<tr>
<td>15</td>
<td>54.5</td>
<td>969.8</td>
<td>175.6 k</td>
<td>1.02</td>
</tr>
<tr>
<td>20</td>
<td>55.4</td>
<td>981.2</td>
<td>175.6 k</td>
<td>1.02</td>
</tr>
<tr>
<td>25</td>
<td>55.9</td>
<td>988.2</td>
<td>175.6 k</td>
<td>1.02</td>
</tr>
</tbody>
</table>

**IV. DISCUSSION FOR VARIATION IN Q**

The circuit performance was studied with different values of $Q$ ($Q = 0.2, 0.5, 1.2, 2, 5, 10, 15, 20, 25$). The observed frequency response shows good agreement with theoretical results. Following observations are noticed from experimental study at three different terminals; low pass, band pass and high pass filter function for different $Q$.

**V. RESULT AND DISCUSSION**

**a) Low pass response:**

![Low Pass Response](image1)

Figure 2: Low pass (LP) responses for different values of $Q$.

Low pass (LP) responses for different values of $Q$ are shown in figure 2. The observed centre frequency is also in good agreement with the designed value. It is noticed that this circuit has high passband gain and it increases with increase in $Q$ value and is constant for $Q > 10$. Gain roll off per octave is excellent for $Q > 1.2$. The %Change in $F_{OL}$ decreases with $Q$ value. Overshoot is observed and increases for $Q > 1.2$. The circuit shows excellent performance for $Q > 10$.

**b) Band pass response:**

![Band Pass Response](image2)

Figure 3: The band pass (BP) response for different $Q$. 

- The circuit shows excellent performance for $Q > 10$. 

- Gain roll off per octave is excellent for $Q > 1.2$. 

- Overshoot is observed and increases for $Q > 1.2$. 

- The %Change in $F_{OL}$ decreases with $Q$ value.
The band pass (BP) response for different $Q$ is shown in figure 3. The Maximum passband gain increases with $Q$ value. The bandwidth is slightly deviated from central frequency value. It is observed that curves are symmetric on both sides. The circuit shows excellent performance for higher values of $Q$.

c) High pass response:

![High Pass Response for Central Frequency 10 kHz](image)

Figure -4 : High pass (HP) responses for different values of $Q$

High pass (HP) responses for different values of $Q$ are shown in figure 4. The response shows that GRPO is excellent and close to ideal value for higher $Q$ values. For $Q \geq 5$ gain stabilizes at 0 dB. The circuit shows ideal response for $Q \geq 10$.

VI. CONCLUSION

A realization of voltage mode transfer function for a third-order active-R filter using op.amp. with multiple feedback signal has been presented. This circuit is composed only of three op. amplifiers and four resistances. Also, this single filter circuit gives three filter functions; low pass, band pass and high pass. The low pass and band pass performance of the circuit gives high passband gain and excellent GRPO for higher value of $Q$. For high pass filter, circuit shows gain stabilization at 0 dB for higher values of $Q$. Low pass, Band pass and High pass filter works excellent for higher values of $Q$.

REFERENCES