

## CB Based Approach for Mining Frequent Itemsets

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**ABSTRACT :** In this paper, we propose a new method for discovering frequent itemsets in a transactional data stream under the sliding window model. Based on a theory of Chernoff Bound, the proposed method approximates the counts of itemsets from certain recorded summary information without scanning the input stream for each itemset. Together with an innovative technique called dynamically approximating to select parameter-values properly for different itemsets to be approximated, our method is adaptive to streams with different distributions. Our experiments show that our algorithm performs much better in optimizing memory usage and mining only the most recent patterns in very less time performance with pretty accurate mining result.

**Keywords:** Chernoff Bound, DataStream, Frequent Itemsets

### I. INTRODUCTION

The most significant tasks in data mining are the process of mining frequent itemsets over data streams. It should support the flexible trade-off between processing time and mining accuracy. Mining frequent itemsets in data stream applications is beneficial for a number of purposes such as knowledge discovery, trend learning, fraud detection, transaction prediction and estimation [1]. However, the characteristics of stream data – unbounded, continuous, fast arriving, and time-changing – make this a challenging task.

In data streams, new data are continuously coming as time advances. It is costly even impossible to store all streaming data received so far due to the memory constraint. It is assumed that the stream can only be scanned once and hence if an item is passed, it can not be revisited, unless it is stored in main memory. Storing large parts of the stream, however, is not possible because the amount of data passing by is typically huge. In this paper, we study the problem of finding frequent items in a continuous stream of items. Many real-world applications data are more appropriately handled by the data stream model than by traditional static databases. Such applications can be: stock tickers, network traffic measurements, transaction flows in retail chains, click streams, sensor networks and telecommunications call records. In the same way, as the data distribution are usually changing with time, very often end-users are much more interested in the most recent patterns [3]. For example, in network monitoring, changes in the past several minutes of the frequent patterns are useful to detect network intrusions [4].

Many methods focusing on frequent itemset mining over a stream have been proposed. [13] proposed *FPStream* to mine frequent itemsets, which was

efficient when the average transaction length was small; used lossy counting to mine frequent itemsets; [7],[8], and [9] focused on mining the recent itemsets, which used a regression parameter to adjust and reflect the importance of recent transactions; [27] presented the *FTP-DS* method to compress each frequent itemset; [10] and [1] separately focused on multiple-level frequent itemset mining and semi-structure stream mining; [12] proposed a group testing technique, and [15] proposed a hash technique to improve frequent itemset mining; [16] proposed an in-core mining algorithm to speed up the runtime when distinct items are huge or minimum support is low; [15] presented two methods separately based on the average time stamps and frequency-changing points of patterns to estimate the approximate support of frequent itemsets; [5] focused on mining a stream over a flexible sliding window; [11] was a block-based stream mining algorithm with *DSTree* structure; [12] used a verification technique to mine frequent itemsets over a stream when the sliding window is large; [11] reviewed the main techniques of frequent itemset mining algorithm over data streams and classified them into categories to be separately addressed.

The above methods are mostly based on the  $(\epsilon, \delta)$  approximation scheme, and depend on error parameter  $\epsilon$  to control the memory consumption and the running time. While a dilemma between mining precision and memory consumption will be caused by the error parameter  $\epsilon$ . A little decrease of  $\epsilon$  may make memory consumption large, and a little increase of  $\epsilon$  may degrade output precision. Since uncertain streams are highly time-sensitive, most data items are more likely to be changed as time goes by, besides people are generally more interested in the recent data items than those in the past.

Thus this needs an efficient model to deal with the time-sensitive items on uncertain streams. Sliding-window model is the most comprehensive approach to coping with the most recent items in many practical applications. So we introduce a Chernoff bound with Markov's inequality to deal with this problem.

The remainder of this paper is organized as follows. In Section 2, we give an overview of the related work and present our motivation for a new approach. Section 3 goes deeper into presenting the problems and gives an extensive statement of our problem. Section 4 presents our solution. Experiments are reported in Section 5, and Section 6 concludes the paper with the features of our work.

### II. RELATED WORK

Many previous studies contributed to the efficient mining of frequent itemsets (FI) in streaming data [4, 5]. According to the stream processing model [20], the research of mining frequent itemsets in data streams can be divided into three categories: landmark windows [15,

12, 19, 11, 13], sliding windows [5, 6, 14, 16, 17, 18], and damped windows [7, 4], as described briefly as follows. In the landmark window model, knowledge discovery is performed based on the values between a specific timestamp called landmark and the present. In the sliding window model, knowledge discovery is performed over a fixed number of recently generated data elements which is the target of data mining.

According to the existential uncertain stream model, an uncertain stream  $US$  is a continuous and unbounded sequence of some transactions,  $\{T_1 T_2 \dots T_n \dots\}$ . Each transaction  $T_i$  in  $US$  consists of a number of items, and each item  $x$  in  $T_i$  is associated with a positive probability  $PT_i(x)$ , which stands for the possibility (or likelihood) that  $x$  exists in the transaction  $T_i$ . For a given uncertain stream, there are many possible instances called worlds that are carried by the stream. The possible worlds semantics has been widely used in [8, 9], which can be adopted in this paper to illustrate uncertain streams clearly. Each probability  $PT_i(x)$  associated with an item  $x$  deduces two possible worlds,  $pw_1$  and  $pw_2$ . In possible world  $pw_1$ , item  $x$  exists in the transaction  $T_i$ , and in possible world  $pw_2$ , item  $x$  does not exist in  $T_i$ . Each possible world  $pw_i$  is annotated with an existence probability, denoted as  $P(pw_i)$  that the possible world  $pw_i$  happens. By this semantics, we can get  $P(pw_1)=PT_i(x)$  and  $P(pw_2)=1-PT_i(x)$ . In fact, a transaction often contains several items.

We introduce a new approach which combines the mathematical model Chernoff bound for this problem. The main attempts were to keep some advantages of the previous approach and resolve some of its drawbacks, and consequently to improve run time and memory consumption. We also revise the Markov's inequality, which avoids multiple scans of the entire data sets, optimizing memory usage, and mining only the most recent patterns. In this paper, we propose a remarkable approximating method for discovering frequent itemsets in a transactional data stream under the sliding window model. Based on a theory of Combinatorial Mathematics, the proposed method approximates the counts of itemsets from certain recorded summary information without scanning the input stream for each itemset.

### III. PROBLEM DESCRIPTION

The problem of mining frequent itemsets was previously defined by [1]: Let  $I = \{i_1, i_2, \dots, i_m\}$  be a set of literals, called items. Let database  $DB$  be a set of transactions, where each transaction  $T$  is a set of items such that  $T \subseteq I$ . Associated with each transaction is a unique identifier, called its  $TID$ . A set  $X \subseteq I$  is also called an itemset, where items within are kept in lexicographic order. A  $k$ -itemset is represented by  $(x_1, x_2, \dots, x_k)$  where  $x_1 < x_2 < \dots < x_n$ . The support of an itemset  $X$ , denoted  $support(X)$ , is the number of transactions in which that itemset occurs as a subset. An itemset is called a frequent itemset if  $support(X) \geq \sigma \times |DB|$  where  $\sigma \in (0, 1)$  is a user-specified minimum support threshold and  $|DB|$  stands for the size of the database.

The problem of mining frequent itemsets is to mine all itemsets whose support is greater or equal than

$\sigma \times |DB|$  in  $DB$ . The previous definitions consider that the database is static. Let us now assume that data arrives sequentially in the form of continuous rapid streams. Let data stream

$DS = B^{b_1}, B^{b_1+1}, \dots, B^{b_n}$  be an infinite sequence of batches,  $a_i, a_{i+1}, \dots, a_n$

where each batch is associated with a time period  $[a_k, b_k]$ , i.e.

$B^{b_k}$ , and let  $a_n$  be the most recent batch

Each batch  $B_{ak}$  consists of a set of transactions; that is, Each batch  $B_{bk} = [T_1, T_2, T_3, \dots, T_k]$ . We also assume that batches do not have necessarily the same size. Hence, the length

The support of an itemset  $X$  at a specific time interval  $[a_i, b_i]$  is now denoted by the ratio of the number of customers having  $X$  in the current time window to the total number of customers. Therefore, given a user-defined minimum support, the problem of mining itemsets on a data stream is thus to find all frequent itemsets  $X$  over an arbitrary time period  $[a_i, b_i]$ , i.e. verifying:

$$support_t(X) \geq \sigma \times |B_{bi}|, t=a_i$$

of the streaming data using as little main memory as possible. Given a transaction sets  $X$ , we are interested in finding strong bounds

$$\text{Low End: } \Pr[X < a]$$

$$\text{High End: } \Pr[X \geq a]$$

Lemma 1.1 (Markov's Inequality) Let  $X$  be a non-negative random variable (transaction sets) with finite expectation  $\mu$ . Then for any  $\alpha > 0$ :  $\Pr[X \geq \alpha] \leq \mu/\alpha$ .

Lemma 1.2 (Chebyshev's Inequality) Let  $X$  be a random variable (transaction sets) with finite expectation  $\mu$  and standard deviation  $\sigma$ . Then for any  $\alpha > 0$ :  $\Pr[|X - \mu| \geq \alpha \sigma] \leq 1/\alpha^2$ .

Chebyshev's inequality follows from Markov's inequality for the variable  $Y = (X - \mu)^2$  (so  $E[Y] = \text{Var}[X]$ ) and the fact that  $x \rightarrow x^2$  is a strictly monotonic function on  $R_0$ .

$$\Pr[|X - \mu| \geq \alpha \sigma] = \Pr[(X - \mu)^2 \geq \alpha^2 \sigma^2]$$

$$\leq \frac{E[(X - \mu)^2]}{\alpha^2 \sigma^2} = 1/\alpha^2$$

This makes it tempting to use even higher moments to get better bounds. One way to do this nicely is by considering an exponential of the basic form of  $e^x$ .

Proof. Lemma 1.3 (Simplified Chernoff Bounds)

Low End:

$$\Pr[X < (1 - \delta)\mu] < e^{-\mu\delta^2/2} \quad 0 < \delta \leq 1$$

High End:

$$\Pr[X \geq (1 + \delta)\mu] < e^{-\mu\delta^2/3} \quad 0 < \delta \leq 1$$

$$\Pr[X \geq (1 + \delta)] < e^{-(1+\delta)\mu} 2e - 1 < \delta$$

Proof.

For the LowEnd let  $D = (1 - \delta)^{1-\delta}$ . By Taylor expansion we get

$$\begin{aligned} \ln D &= (1 - \delta) \ln(1 - \delta) \\ &= (1 - \delta)(-\delta - \delta^2/2 - \delta^3/3 - \dots) \\ &= -\delta + \delta^2/2 + \delta^3/6 + \dots \\ &> -\delta + \delta^2/2 \end{aligned}$$

By Applying this simplified method in the series we can get the following equation for low end windows.

$$\text{Hence } \left( \frac{e^{-\delta}}{(1 - \delta)^{1-\delta}} \right) = e^{-\mu\delta/2}$$

#### IV. CBMFI ALGORITHM

CBMFI (Chernoff Bound Based Mining Frequent Itemsets) algorithm relies on a verifier function and it is an exact and efficient algorithm for mining frequent itemsets sliding windows over data streams. The performance of CBMFI improves when small delays are allowed in reporting new frequent itemsets, however this delay can be set to 0 with a small performance overhead.

The following algorithm shows how it combines with CB for Mining frequent itemsets.

#### CBMFI

Initialization

For all  $u$  pick a route  $rt(u)$ .

Place all  $M_u$  such that  $D(u) = \mu u$  into  $C_e$  where  $e$  is the first window on  $rt(u)$ .

Main Loop  $r = 0$

while( there is a packet not at its destination )

in parallel, for all window ends  $e = (x, y)$

do

if  $C_e$  is not empty,

pick the highest priority itemsets in  $C_e$

$y = \text{itemsets}(T)$

if ( a moved itemset is not at its destination )

$C_e = \text{next end transaction}$

$r = r + 1$

We would like to use a Chernoff bound, so we need to find some independent Poisson trials somewhere. This requires a bit of thought, lots of random variables associated with this algorithm are not independent;

The expected length of a route is  $k/2$ , so the total number of edges on all routes is expected to be  $nk/2$ . The total number of edges in a hypercube is  $nk$ , so we have  $E[R(e)] = 1/2$ . It follows that  $E[H] \leq k/2$ . Now apply the simplified Chernoff bound where  $\delta > 2e - 1$ :

$$\Pr[H \geq 6k] < 2 - 6k$$

This is allowed since  $6k = (\delta + 1)\mu$  implies  $\delta > 11$ . By applying this in the CBMFI algorithm we can get the efficient result.

#### V. EXPERIMENTAL RESULTS

All experiments were implemented with C#, compiled with Visual Studio 2005 in Windows Server 2003 and executed on a Xeon 2.0GHz PC with 4GB RAM. We used 1 synthetic datasets and 1 real-life datasets, which are well-known benchmarks for frequent itemset mining. The T40I10D100K dataset is generated with the IBM synthetic data generator.

We firstly compared the average runtime of these two algorithms under different data sizes when the minimum support was fixed. As shown in all of the images in Fig.5.1, the running time cost of MFI and CBMFI increase following the data size; these results verify that both algorithms are sensitive to data size, which is due to the using of unchanged absolute minimum support

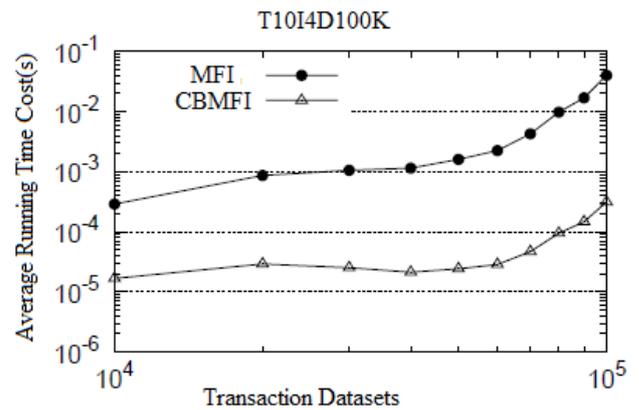


Fig: 5.1 Runtime vs number of Records

#### Memory Cost Evaluation

To evaluate the memory cost of our algorithm, we compared the count of generated items in MFI and CBMFI. As shown in Fig.5.2 and Fig.5.3, when we fix the minimum support and increase the data size, the generated items of both algorithms become more, but the overall item count of CBMFI is less than that of MFI since CBMFI uses a simplified method for itemsets.

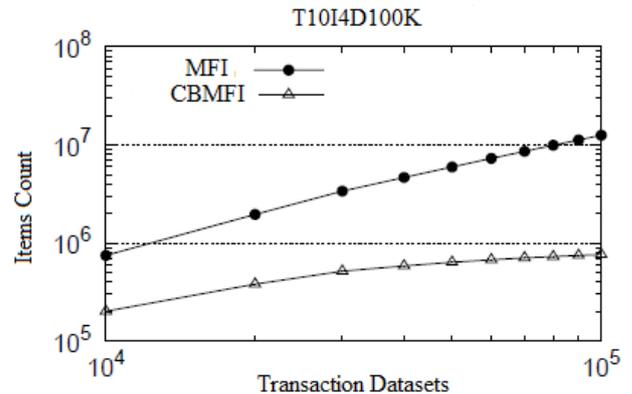


Fig: 5.2 Itemset Count cost vs Transaction Set

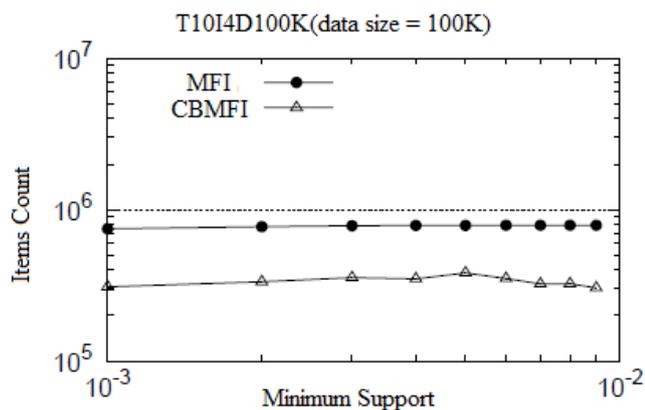


Fig: 5.3 Itemssets Count cost vs. Minimum Support

Furthermore, when the minimum support increases, the incremental scope of *CBMFI* is much reduced than that of *MFI*, that is because more redundant items when the overall items count is fixed but the itemsets count increases.

## VI. CONCLUSION

In this paper we considered a problem that how to mine frequent itemset over stream sliding window using Chernoff Bound. We compared two algorithms *MFI* and *CBMFI* and introduce a compact data structure, which can compress the itemset storage and optimize itemset computation, based on combinatorial mathematical. Our experimental studies showed that our algorithm is effective and efficient.

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